

Arc Length Formula	Explanation
$L = \int_a^b \sqrt{1 + [f'(x)]^2} dx$	Arc length of “nice functions” with respect to $x$ .

1. Find the length of the following curves.

(a)  $\frac{3}{4}x - \frac{1}{4}, \quad -1 \leq x \leq 3.$

(b)  $12x = 4y^3 + 3y^{-1}, \quad 1 \leq y \leq 3.$

2. Find  $b$  such that the length of the curve  $y = 1 + 6x^{3/2}$ ,  $0 \leq x \leq b$ , is 6.

Surface Area Formula	Explanation
$S = \int_a^b 2\pi f(x) \sqrt{1 + [f'(x)]^2} dx$	Surface area of “nice functions” rotated about the $y$ -axis.

3. Find the surface areas obtained in the following situations.

(a) rotating the curve  $f(x) = \sqrt{1 + e^x}$  for  $0 \leq x \leq 1$  around the  $x$ -axis.

(b) rotating the curve  $f(y) = \sqrt{a^2 - y^2}$  for  $0 \leq y \leq a/2$  and  $a$  constant around the  $y$ -axis